**Function model synthesis from code traces**

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ABSTRACT

This research investigates development of a proof of concept named Exemplar[1] that attempts to broaden where PbE can be applied by requiring, along with input and output, code traces that justify each step in the conversion from input to output. Also involved (in this conversion of use case code traces into models of satisfying general functions) are deduction, interrogation of the user, and search. The resulting functions come with a suite of useful unit tests, and are easy to polish from model into finished function.

BACKGROUND

Once a programmer decides what a program should do, programming becomes the discovery of the precise mechanism that will behave as desired under all legal inputs. This task is much harder for the programmer than simply specifying desired output given the exemplary inputs for a limited number of use cases. As a result, satisfactory mechanisms for robust and comprehensive “programming by example” (PbE) systems have long been sought, but with little success beyond tightly circumscribed application areas such as resolving points of programmer uncertainty in an algorithm by search[2], or deriving spreadsheet formulae by deduction[3].

At the same time, it is common for coders to complete code traces on paper as part of the design phase before a significant programming implementation.

Therefore, it would greatly facilitate programming if these two elements, viz., traced use cases along with their starting input and ultimate output, could form the basis of automatic derivation of programs. It is believed that the presently described system lays such a foundation.

DISCUSSION

Exemplar’s central innovation is to attack the core problem PbE systems face, viz., the disambiguation of a desired algorithm from little more than context and input and output example pairs, by introducing two compromises, (code trace) assertions, and straightforward questions put to the user.

How Exemplar works, to the user

Exemplar is designed to free the coder from having to initially think about how to solve a task generally, or having to carefully plot control structures, and instead simply take a mental walk through the conditions that must be true for the concrete values and conditions in his/her use cases. These form the code trace assertions required by Exemplar.

These are shown below. Exemplar’s runs usually also include multiple choice questions put to the user. Such questions appear wherever necessary to confirm which of the possible generalizations are desired. The answers are recorded for subsequent runs of Exemplar against an input file of the same name.

Below are two in depth demonstrations of Exemplar.

Imagine that we want Examplar to generate a function that returns whether a given integer is prime. That requires a code trace from the user, which can be submitted to Exemplar as a file named prime\_number.exem. It follows.

<1008 # Assertion-less user examples are considered for testing purposes   
>False # (and not function synthesis).  
  
<0  
i1==inp # i1 is the default variable name. (Just “inp” is sufficient to rename.)

inp <= 1 # This means that, because inp is <=1, we:  
>False # return False.  
  
<1  
i1==inp   
inp <= 1 # Ditto.  
>False  
  
<3   
>True  
  
<4  
i1==inp # Renaming i1 (the default name given to input) is good practice.  
inp > 1  
j == 2 # FOR loop with only one iteration in this example because  
inp % j == 0 # inp divides evenly. And so we have an answer:  
>False # not prime.  
  
<5  
i1==inp  
inp > 1 # Since inp is > 1, the following (j) loop is reached.  
j==2  
# (N.B. inp % j != 0, <4 example’s condition NOTed, is \*not\* traced here because

# that truth does not trigger any code.)  
j==3 # j is simply incremented, until it  
j==4  
j==5  
j==inp # reaches the value of inp, at which point we conclude that inp is:  
>True # prime.

To decipher the above, Exemplar attempts to wind up the loop iterations that the user’s examples imply into a self-consistent ball of Python code, phrased as a function. In this case, that synthesized function is a primality predicate. Like all of Exemplar’s synthesized functions, it is embedded in a unittest suite. I.e., file TestPrimeNumber.py is created with contents

*# AUTOGENERATED FILE -- RENAME OR YOUR EDITS WILL BE OVERWRITTEN***import** unittest, exemplar  
actual\_io\_trace = **''** *# Receives test values print()'ed and input().*global\_input = [] *# Assigned in each test to provide input() values to the function under test.  
  
  
# print() is mocked to see if the tests recreate the .exem-specified i/o in actual\_io\_trace.***def** print(line=**""**) -> **None**:  
 **global** actual\_io\_trace  
 **if** line **is** str:  
 line = line.translate(str.maketrans({**"'"**: **r"\'"**})) *# Escape single quotes* actual\_io\_trace += **">"** + str(line) + **'\n'***# input() is mocked to return the test-specified input as well as add it to actual\_io\_trace.***def** input(variable\_name: str = **""**) -> str:  
 *# (variable\_name is ignored because it may not have been specified by the .exem.)* **global** actual\_io\_trace  
 result = global\_input.pop(0)  
 result = result.translate(str.maketrans({**"'"**: **r"\'"**})) *# Escape single quotes* actual\_io\_trace += **"<"** + result + **'\n'** *# Eg, '<Albert\n'* **return** result  
  
  
*# The generated function under Stage 2 (i.e., a test per example) testing.***def** prime\_number():  
 inp = int(input(**"inp:"**)) *# Eg, 0* **if** inp<=1:  
 print(**'False'**)  
 **return 'False'   
 elif** inp>1:  
 **for** j **in** range(2, 6, 1):  
 **if** j==inp:  
 print(**'True'**)  
 **elif** inp%j==0:  
 print(**'False'**)  
 **break  
  
  
class** TestPrimeNumber(unittest.TestCase):  
  
 **def** setUp(self):  
 **global** actual\_io\_trace  
 actual\_io\_trace = **''** self.maxDiff = **None  
  
 def** test\_prime\_number3(self):  
 **global** global\_input  
 global\_input = [**'1008'**] *# From the .exem* prime\_number() *# The function under test is used to write to actual\_io\_trace.* self.assertEqual(**'''<1008  
>False  
'''**, actual\_io\_trace)  
  
 **def** test\_prime\_number8(self):  
 **global** global\_input  
 global\_input = [**'0'**] *# From the .exem* prime\_number() *# The function under test is used to write to actual\_io\_trace.* self.assertEqual(**'''<0  
>False  
'''**, actual\_io\_trace)  
  
[This continues, one test per user example.]  
  
**if** \_\_name\_\_ == **'\_\_main\_\_'**:  
 unittest.main()

That generated function again:

1. **def** prime\_number():
2. inp = int(input(**"inp:"**)) *# Eg, 0*
3. **if** inp<=1:
4. print(**'False'**)
5. **return 'False'**
6. **elif** inp>1:
7. **for** j **in** range(2, 6, 1):
8. **if** j==inp:
9. print(**'True'**)
10. **elif** inp%j==0:
11. print(**'False'**)
12. **break**

How and why Exemplar created each line:

1. The function’s name, prime\_number, is taken from the input file.
2. All the user examples started with an integer input, thus this line.
3. Each example has one of two IF assertions in this position. This assertion Exemplar saw first, so it is coded into Python above its sibling IF branch.
4. Both examples with line 3’s IF assertion follow it with output of False. (There’d be an inconsistency error if not.)
5. return is implied by the conforming examples’ final print().
6. This is the 2nd IF condition seen in the examples.
7. Each of the examples with line 6’s IF condition are followed with a FOR loop ranging up to 6 – 1.
8. Those FOR loop instances start with IF conditions of j==inp or inp%j==0. In the case of the former,
9. True is output.
10. In the user examples with this IF condition,
11. False is output and the
12. FOR loop ends early, implying this break.

N.B. A shortcoming in this rendition of prime\_number() is that the FOR loop’s encoded range() matches that of the longest user example rather than being a WHILE loop that iterates as long as it takes to determine primality. This limitation cannot be overcome until Exemplar again implements WHILE loops, a planned improvement.

Here is another problem Exemplar solves, a child’s guessing game [4]. A code trace that works for this is

# User wins.  
>Hello! What is your name?  
<Albert  
name==i1   
>secret = random.randint(1,20)  
<4  
secret==i1   
>Well, Albert, I am thinking of a number between 1 and 20.  
guess\_count==0   
>Take a guess.  
<10  
guess==i1, guess>secret # Assertions can be comma delimited.  
>Your guess is too high.  
guess\_count == 1 # Repeating the guess\_count=<integer> scheme indicates iteration.  
>Take a guess.  
<2  
guess==i1, guess<secret   
>Your guess is too low.  
guess\_count==2 # iteration  
>Take a guess.  
<4  
guess==i1, guess==secret   
guess\_count + 1 == 3   
>Good job, Albert! You guessed my number in 3 guesses!  
  
  
# User loses.  
>Hello! What is your name?  
<John  
name==i1  
>secret = random.randint(1,20)  
<3  
secret==i1  
>Well, John, I am thinking of a number between 1 and 20.  
guess\_count==0  
>Take a guess.  
<11  
guess==i1, guess>secret  
>Your guess is too high.  
guess\_count == 1  
>Take a guess.  
<1  
guess==i1, guess<secret  
>Your guess is too low.  
guess\_count==2  
>Take a guess.  
<2  
guess==i1, guess<secret  
>Your guess is too low.  
guess\_count==3  
>Take a guess.  
<10  
guess==i1, guess>secret  
>Your guess is too high.  
guess\_count==4  
>Take a guess.  
<9  
guess==i1, guess>secret  
>Your guess is too high.  
guess\_count==5  
>Take a guess.  
<8  
guess==i1, guess>secret  
>Your guess is too high.  
guess\_count >=5 # User avoids guess\_count==5, as that'd look like another iteration.  
>Nope. The number I was thinking of was 3.

From that Exemplar produces function

**def** guess4():  
 print(**'Hello! What is your name?'**)  
 name = input(**"name:"**) *# Eg, Albert* print(**'secret = random.randint(1,20)'**)  
 secret = int(input(**"secret:"**)) *# Eg, 4* print(**'Well, '** + str(name) + **', I am thinking of a number between 1 and 20.'**)  
 **for** guess\_count **in** range(0, 6, 1):  
 print(**'Take a guess.'**)  
 guess = int(input(**"guess:"**)) *# Eg, 10* **if** guess>secret:  
 print(**'Your guess is too high.'**)  
 **elif** guess<secret:  
 print(**'Your guess is too low.'**)  
 **elif** guess==secret:  
 print(**'Good job, '** + str(name) + **'! You guessed my number in '** + str(guess\_count+1) + **' guesses!'**)  
 **break  
 if** guess\_count>=5:  
 print(**'Nope. The number I was thinking of was '** + str(secret) + **'.'**)

That function is produced by the same inference mechanisms described for the prime\_number example, with the additional feature that questions are asked of the user at .exem submission time. Those are

Immediately after lines   
 elif guess==secret:  
 print('Good job, ' + str(name) + '! You guessed my number in ' + str(guess\_count+1) + ' guesses!')  
 break  
 if guess\_count>=5:  
which transformation?   
1) print('Nope. The number I was thinking of was 3.')  
2) print('Nope. The number I was thinking of was ' + str(secret) + '.')  
2  
  
Immediately after lines   
 print('Your guess is too high.')  
 elif guess<secret:  
 print('Your guess is too low.')  
 elif guess==secret:  
which transformations? Please enter the sum of your selected choices:   
1) print('Good job, Albert! You guessed my number in 3 guesses!')  
2) print('Good job, ' + str(name) + '! You guessed my number in 3 guesses!')  
4) print('Good job, Albert! You guessed my number in ' + str(guess\_count+1) + ' guesses!')  
6  
  
Immediately after lines   
 print('Hello! What is your name?')  
 name = input("name:") # Eg, Albert  
 print('secret = random.randint(1,20)')  
 secret = input("secret:") # Eg, 4  
which transformation?   
1) print('Well, Albert, I am thinking of a number between 1 and 20.')  
2) print('Well, ' + str(name) + ', I am thinking of a number between 1 and 20.')  
2

The user’s answer to the first and last questions teach Exemplar to use variable output, not a hard-coded 3 or “Albert”. The second answer, 6, is the sum of 2 and 4, meaning that the target function should use a variable name (transformation 2) and variable number (transformation 4) when congratulating a winning player.

Those questions and the user’s answers (2, 6, 2) are stored together in a “.qa” file for subsequent retrieval by Exemplar each time a code trace file with the same name (guess4.exem) is submitted for TestGuess4.py file generation.

N.B. random.randint() is modelled as an output in the .exem and not actually called because the result of doing so would be nondeterministic absent complicating controls cost ineffective in a proof of concept.

**How Exemplar works, internally**

Each time exemplar.py is run, a code trace (.exem file) must be specified as an argument.

Then exemplar.py’s \_\_main\_\_ section launches a function named reverse\_trace() that resets the (Sqlite) database, pulls the code trace lines from .exem file, and inserts them into the database.

The body of reverse\_trace() (edited for clarity):

reset\_db()  
example\_lines = from\_file(file)  
fill\_example\_lines(example\_lines) *# Insert the .exem's lines into the database.*fill\_conditions\_table() *# The table of user assertions aka truth.*store\_fors()code, test\_file\_contents, success = **get\_function**(file)**return** code, test\_file\_contents

Even though data is not persisted beyond an execution of Exemplar, the consistent interface (SQL) onto the rows of the user examples, as they are evolved into code, proves useful. Even more helpful has been the ability to create database savepoints and rollback when an interpretation of the examples results in error or inconsistency.

After the example\_lines table is filled, fill\_conditions\_table() heuristically categorizes all the assertions as either assignment, IF condition, or FOR condition.

Then store\_fors() runs (a function difficult to write due to all the order-sensitive state changes) correctly compiles a virtual dossier on each FOR block, noting their starting point, first potential stopping point, and final potential stopping point.

Everything that Exemplar does after store\_fors() is orchestrated by get\_function().

get\_function() first pulls a complete set of potential FOR loop stopping points (via get\_last\_el\_id\_maybes()), begins a database transaction, then instantiates those potential stopping points in a temporary database table. If any of the conjectured stopping points prove untenable, the transaction is rolled back , and another set of potential stopping points is pulled (again via get\_last\_el\_id\_maybes()).

Nested under this procedure is the equivalent process, only for IF controls. I.e., store\_ifs(), a function much like store\_fors(), compiles information on each IF block, noting each IF block’s starting point, first potential stopping point, and last possible stopping point. From this potential pool, a definite endpoint is conjectured for each IF block and another database transaction (nesting into one started by the lastest FOR loop interpretation) starts, and these endpoints are written to a temporary database table. Again, as with FOR blocks, as soon as an inconsistency is detected, the latest transaction (only) is rolled back and a new set of potential IF endpoints is trialed.

When an interpretation of FOR loops and IF blocks reaches generate\_code(), a target function is synthesized via the reasoning outlined in the preceding section (How Exemplar works, to the user).

At the end of generate\_code(), the target function’s IF branches are re-ordered until all examples pass. That doesn’t involve testing the full function, just setting the state to match a particular IF branching point in each user example, and seeing if the IF branch triggered in an eval() matches that of the user example.

An interesting function involved in this is get\_IF\_permutation(), in that it uses factoradics [5] to number and track the IF branch orderings.

After generate\_code(), generate\_tests() creates the test suite and the resulting unit tests are executed against the synthesized function. If all tests pass, the target function is triumphantly returned. Otherwise, the latest database transaction is rolled back and the next set of control structure endpoints are trialed. This continues until success (no errors) or there are no more endpoints to try, in which case the database changes are committed for post mortem analysis, and failure is reported to the user.

**SUMMARY**

The process of working out a program can be made by a metaprogram automatically discovering the code that correlates to exemplary, traced, use cases provided by the programmer*.* This saves programming time even if the resulting function only models the desired program via its correct control structures, as it should then be relatively easy for the programmer to polish the program into a final, desired form.

The present work resolved PbE’s problem of ambiguity by a combination of approaches:

1. Novelly, by requiring code trace assertions that “hint” as to why a certain path through the algorithm is chosen in a particular case.
2. Generate-and-testing code until it reproduces sample output from sample input, to induce each control structure’s endpoint in the given trace.
3. Deducing all conclusions that the example code traces make possible.
4. Confirming possible generalizations by asking the user a multiple choice question and saving the answers.

**References**

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